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clc;
close all;
clear;

%% Input Geometry && Definitions
% Geometry
Nodes=3.6*[2,1;2,0;1,1;1,0;0,1;0,0]; % Nodes
(m)
Con=[5 3;1 3;6 4;4 2;4 3;2 1;6 3;5 4;4 1;3 2]; % Connectivity
% Material
E=21000000*ones(1,size(Con,1)); % Young's Modulus in t/m2
A=42.6*10^-4*ones(1,10); % Area of each member in m
% Temperature

% Forces
F=zeros(2*size(Nodes,1),1); % Global force vector with setting reactions to zero
F(4,1)=-100; % Forces in ton
F(8,1)=-100;
% Supports
Sup_DOF = [9 10 11 12]; % Global DOFs for supports
Prescribed_BC = [0 0 0 0]; % Proscribed value of the displacement

%% Calculations
Tdof=2*size(Nodes,1); % Number of total DOFs
Nelem=size(Con,1); % Number of elements
xi=[Nodes(Con(:,1),1),Nodes(Con(:,1),2)]; % node
Nodesinates i of each element
xj=[Nodes(Con(:,2),1),Nodes(Con(:,2),2)]; % node
Nodesinates j of each element
EA =E.*A; % E*A of each element

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K = zeros(Tdof); % Initialize the global
stiffness matrix
EFT=[2*Con(:,1)-1,2*Con(:,1),2*Con(:,2)-1,2*Con(:,2)];
Ft = zeros(Tdof, 1); % Initialize the global
thermal load vector
L=zeros(Nelem,1); % Intialize length
Vector
c=zeros(Nelem,1); % Intialize Cosine
Vector
s=zeros(Nelem,1); % intialize sine vector

%% Solver
for i=1:Nelem
%% subroutine to compute the element stiffness matrix
Ke
% Compute the element length L
Xij = xj(i,:)-xi(i,:); % Relative Nodes vector from
node i to node j
elbar = Xij/norm(Xij); % Unit vector for the element
axis
c(i) = elbar(:,1); % c is cos(phi)
s(i) = elbar(:,2); % s is sin(phi)
L(i) = norm(Xij);

% Compute cos(phi) and sin(phi) from the nodal
Nodesinates of node i and j
% Compute the Nodesinate transformation matrix T ( T is
a 4x4 matrix)
T = [ c(i) s(i) 0 0
      -s(i) c(i) 0 0
      0 0 c(i) s(i)
      0 0 -s(i) c(i)];
% Compute the local element stiffness matrix Kbar
Kbar = EA(i)/L(i)*[ 1 0 -1 0
                     0 0 0 0
                     -1 0 1 0
                     0 0 0 0];
% Compute the global element stiffness matrix Ke using
T and Kbar
Ke = T'*Kbar*T;

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%% subroutine to compute the element thermal joint
force Fte
% % Ft_bar = alp(i)*EA(i)*dT(i)*[-1 0 1 0]';
% % Compute the global thermal joint force vector Ft
using T and Ft_bar
% % Fte = T'*Ft_bar;

%% Assemble the global stiffness K using EFT
K(EFT(i,:), EFT(i,:)) = K(EFT(i,:), EFT(i,:)) + Ke;
% Assemble the global thermal joint force vector Ft
using EFT
Ft(EFT(i,:)) = Ft(EFT(i,:));
end

% Copy K and F+Ft to Khat and Fhat
Khat = K;
Fhat = F+Ft;
% Modify the global force vector using the prescribed
value of displacement
Us = zeros(Tdof,1);
Us(Sup_DOF) = Prescribed_BC;
Fhat = Fhat - K*Us;
% Make rows and columns of Khat related to supports
zero.
Khat(Sup_DOF, :) = 0;
Khat(:, Sup_DOF) = 0;
% Set the corresponding force components to the
prescribed value of the displacement.
Fhat(Sup_DOF) = Prescribed_BC ;
% Put ones to the diagonals related to supports.
Khat(Sup_DOF, Sup_DOF) = eye(length(Sup_DOF));
% Solve the system of the equations and print out the
solution U
U = Khat\Fhat;
disp('U='); disp(U');
% Compute the reaction forces
F = K*U - Ft;
% Print out the reaction F
disp('F='); disp(F');
% Compute the axial force in each element
for i=1:Nelem

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% Extract the external displacement vector Ue from the
global displacement vector
Ue = U(EFT(i,:));
% Compute the axial force
Pe = EA(i)/L(i)*[-c(i) -s(i) c(i) s(i)]*Ue;
% Print out the axial forces
disp(['P',num2str(i), '=' ,num2str(Pe)]);
end

Sc=10;
Nodes_Modified=Nodes+Sc*reshape(U, [2, 6])';
e=Con(:,1);
f=Con(:,2);

figure()
% axis('square')
hold on
for i=1:length(Con(:,1))
e=Con(i,1);
f=Con(i,2);
X=[Nodes(e,1),Nodes(f,1)];
Y=[Nodes(e,2),Nodes(f,2)];

X2=[Nodes_Modified(e,1),Nodes_Modified(f,1)];
Y2=[Nodes_Modified(e,2),Nodes_Modified(f,2)];

plot(X,Y, 'k')
plot(X2,Y2, '--m')

end
hold off

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